

Schiff-Moment and TPT-Ne Interactions in Mercury and Francium-Silver

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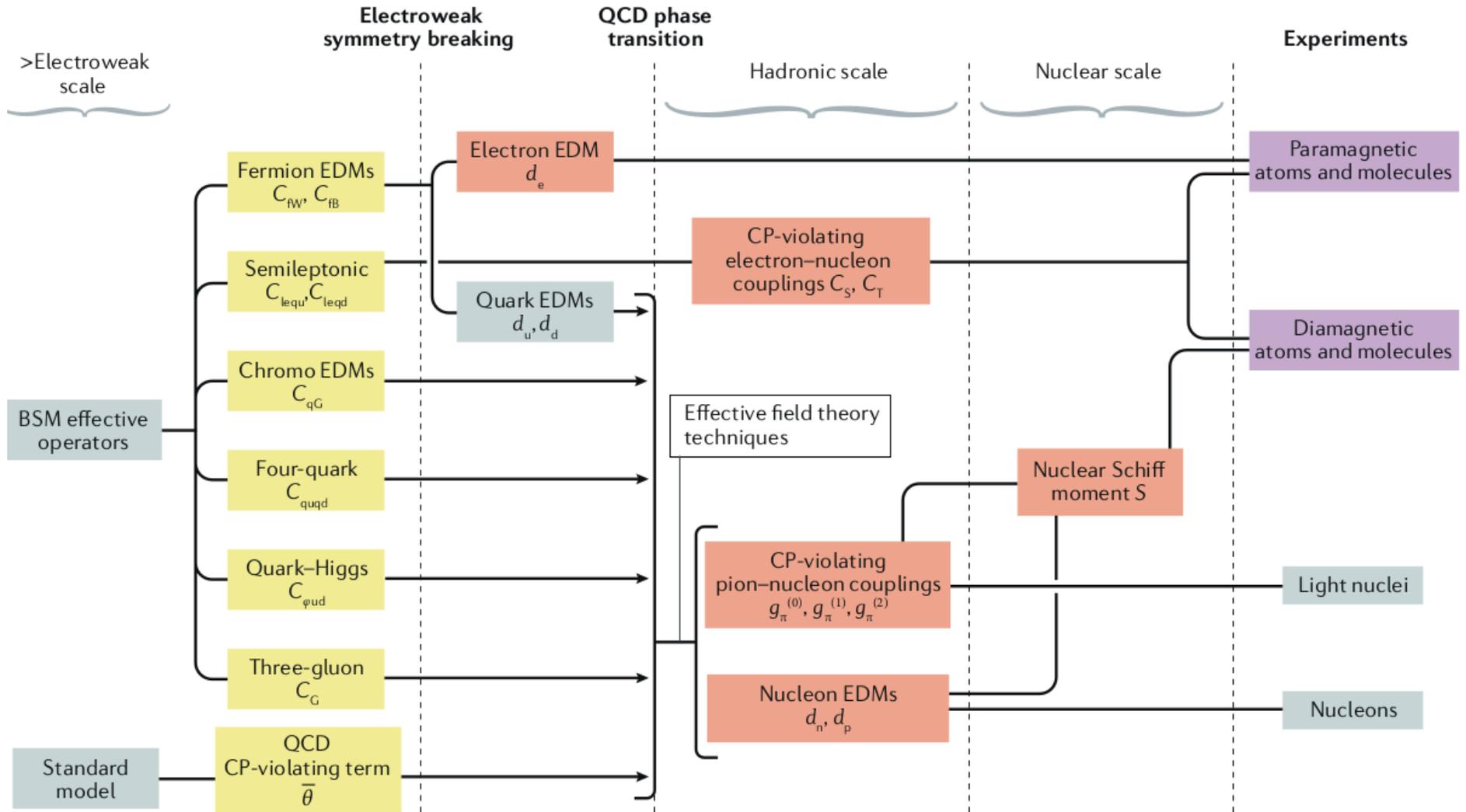
03 March 2026



Laboratoire de Chimie et Physique Quantiques



EDMs and their possible sources: An overview



W. Cairncross, J. Ye, *Nat. Rev. Phys.* **1** (2019) 510

EDM Science

- Electron EDM interactions (HfF^+ , ThO , Hg , Tl , TaO^+ , RaAg et al.)

T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

T. F., L. V. Skripnikov, *Symmetry* **12** (2020) 498

T. F., M. Jung, *J High Energy Phys. (JHEP)* **07** (2018) 012

T. F., *Phys. Rev. A* **96** (2017) 040502(R)

T. F., *Phys. Rev. A* **95** (2017) 022504

M. Denis, T. F., *J. Chem. Phys.* **145** (2016) 214307

- Nuclear Schiff-moment interactions (Xe , Hg , TlF , FrAg et al.)

A. Marc, M. Hubert, T. F., *Phys. Rev. A* **108** (2023) 062815

M. Hubert, T. F., *Phys. Rev. A* **106** (2022) 022817

- Weak neutral current interactions (Xe , Hg , Ra , TlF , FrAg , CsAg)

L. V. Skripnikov, T. F. (2026) *in preparation*

A. Marc, T. F., *Eur. Phys. J. D* **79** (2025) 19

T. F., *Phys. Rev. A* **109** (2024) 022807

T. F., *Phys. Rev. A* **99** (2019) 012515

- Nuclear MQM interactions (TaN , TaO^+ , HfF^+ , RaAg)

T. F., M. K. Nayak, M. G. Kozlov, *Phys. Rev. A* **93** (2016) 012505

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T. F., M. K. Nayak, M. G. Kozlov, *Phys. Rev. A* **93** (2016) 012505

Current World Records

In the presence of a non-zero EDM d , the system's Hamiltonian is

$$\hat{H} = -(\mu\mathbf{B} + d\mathbf{E}) \cdot \frac{\hat{\mathbf{J}}}{|\mathbf{J}|}$$

- **“Paramagnetic” systems:** Precession measurement on **HfF⁺**
JILA group; Ye, Cornell¹
measured $f = (-14.6 \pm 29.7) \mu\text{Hz} \Rightarrow |d_e| \leq 4.1 \times 10^{-30} e \text{ cm}$
- **“Diamagnetic” systems:** Precession measurement on **Hg**
Seattle group; Heckel²
measured $|d_{\text{Hg}}| \leq 7.4 \times 10^{-30} e \text{ cm}$
- **Neutron (n) EDM experiment**
PSI, Switzerland³
measured $|d_n| \leq 1.8 \times 10^{-26} e \text{ cm}$

¹ T. S. Roussy, *et al.*, J. Ye, E. A. Cornell, *Science* **381** (2023) 46

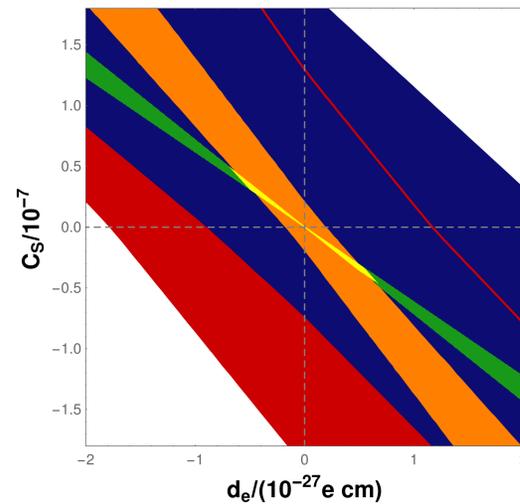
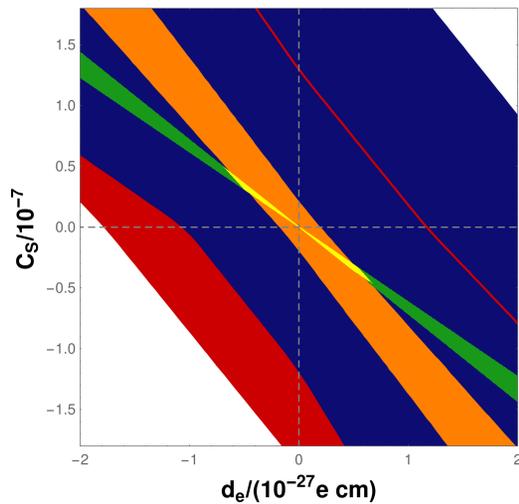
² B. Graner *et al.*, *Phys Rev Lett* **116** (2016) 161601

³ C. Abel *et al.*, *Phys. Rev. Lett.*, **124** (2020) 081803

The TI EDM

T. F., L. V. Skripnikov, *Symmetry* **12** (2020) 498

| Work | α_{de} | $\alpha_{CS}[10^{-18}e\text{ cm}]$ |
|----------------------------------------------|----------------------|------------------------------------|
| Flambaum (semi-empirical) | -500 | |
| Johnson <i>et al.</i> (Norcross potential) | -562 | |
| Mårtensson-Pendrill <i>et al.</i> (estimate) | -600 ± 200 | 7 ± 2 |
| Liu <i>et al.</i> | $-585 \pm (30 - 60)$ | |
| Dzuba <i>et al.</i> | -582 ± 20 | 7.0 ± 0.2 |
| Nataraj <i>et al.</i> (CCSD(T)) | -466 ± 10 | |
| Sahoo <i>et al.</i> (CCSD(T)) | | 4.06 ± 0.14 |
| Porsev <i>et al.</i> | -573 ± 20 | |
| This work CI | -539 ± 33 | 6.61 ± 0.4 |
| This work CC | -559 ± 28 | 6.77 ± 0.34 |



The Hg EDM

T. Chupp, P. Fierlinger, M. J. Ramsey-Musolf, J. T. Singh, *Rev. Mod. Phys.* **91** (2019) 015001

TABLE IV. Coefficients for P -odd and T -odd parameter contributions to EDMs for diamagnetic systems and the neutron. The second line for each entry is the reasonable range for each coefficient. The $\partial d^{\text{exp}}/\partial d_e$ and $\partial d^{\text{exp}}/\partial C_S$ are from Ginges and Flambaum (2004) and are based on Mårtensson-Pendrill (1985) and Mårtensson-Pendrill and Öster (1987) for ^{129}Xe and ^{199}Hg . Also see Fleig and Jung (2018) for ^{199}Hg . The $\partial d^{\text{exp}}/\partial d_e$ and $\partial d^{\text{exp}}/\partial C_S$ for TIF are compiled by Cho, Sangster, and Hinds (1991). The $\partial d^{\text{exp}}/\partial C_T^{(0)}$ are adjusted for the unpaired neutron in ^{129}Xe , ^{199}Hg , and ^{225}Ra using k_T from Ginges and Flambaum (2004) and is consistent with Sahoo (2017). For ^{225}Ra $\partial d^{\text{exp}}/\partial C_T^{(0)}$ is from Dzuba, Flambaum, and Porsev (2009) and Singh and Sahoo (2015a). The $\bar{g}_\pi^{(0)}$, $\bar{g}_\pi^{(1)}$, and \bar{d}_n^{sr} coefficients for atoms and molecules are based on data provided in Table V; the range for ^{225}Ra corresponds to $0 \leq s_n \leq 2 \text{ fm}^2$. For TIF, the unpaired neutron is replaced by an unpaired proton and the “best value” assumes $\bar{d}_p^{sr} = -\bar{d}_n^{sr}$, i.e., mostly isovector in analogy to the anomalous magnetic moment, while the range is defined by $|\bar{d}_p^{sr}| \leq |\bar{d}_n^{sr}|$.

| System | $\partial d^{\text{exp}}/\partial d_e$ | $\partial d^{\text{exp}}/\partial C_S$ (e cm) | $\partial d^{\text{exp}}/\partial C_T^{(0)}$ (e cm) | $\partial d^{\text{exp}}/\partial \bar{g}_\pi^{(0)}$ (e cm) | $\partial d^{\text{exp}}/\partial \bar{g}_\pi^{(1)}$ (e cm) | $\partial d^{\text{exp}}/\partial \bar{d}_n^{sr}$ |
|-------------------|----------------------------------------|-----------------------------------------------|-----------------------------------------------------|-------------------------------------------------------------|-------------------------------------------------------------|---------------------------------------------------|
| Neutron | | | | 1.5×10^{-14} | 1.4×10^{-16} | 1 |
| ^{129}Xe | -0.0008 | -4.4×10^{-23} $-4.4 - (-5.6)$ | -6.1×10^{-21} $-6.1 - (-9.1)$ | -0.4×10^{-19} $-23.4 - (1.8)$ | -2.2×10^{-19} $-19 - (-1.1)$ | 1.7×10^{-5} $1.7-2.4$ |
| ^{199}Hg | -0.014 $-0.014 - 0.012$ | -5.9×10^{-22} | 3.0×10^{-20} $3.0-9.0$ | -11.8×10^{-18} $-38 - (-9.9)$ | 0 $(-4.9 - 1.6) \times 10^{-17}$ | -5.3×10^{-4} $-7.7 - (-5.2)$ |
| ^{225}Ra | | | 5.3×10^{-20} $5.3-10.0$ | 1.7×10^{-15} $6.9-0.9$ | -6.9×10^{-15} $-27.5 - (-3.8)$ | $(-1.6 - 0) \times 10^{-3}$ |
| TIF | 81 | 2.9×10^{-18} | 2.7×10^{-16} | 1.9×10^{-14} $0.5-2$ | -1.6×10^{-13} | 0.46 $-0.5 - 0.5$ |

The Hg EDM

Literature results

| Source | Method | α_{CT} $\left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ |
|-------------------------|---------------------|----------------------------------------------------------------------------------------|
| Mårtensson-Pendrill [4] | HF | -6.0 |
| Dzuba <i>et al.</i> [5] | CI+MBPT | -5.1 |
| Latha <i>et al.</i> [6] | | -4.3 |
| Singh <i>et al.</i> [7] | CCSD _p T | -4.3 |
| Sahoo <i>et al.</i> [8] | RNCCSD | -3.3 |
| T. F. [9] | GAS-CI | -5.0 |

⁴A.-M. Mårtensson-Pendrill, *Phys. Rev. Lett.* **54** (1985) 1153

⁵V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

⁶K. V. P. Latha, D. Angom, B. P. Das, D. Mukherjee, *Phys. Rev. Lett.* **103** (2009) 083001

⁷Y. Singh and B. K. Sahoo, *Phys. Rev. A* **91** (2015) 030501(R)

⁸B. K. Sahoo, B. P. Das, *Phys. Rev. Lett.* **120** (2018) 203001

⁹T. F., *Phys. Rev. A* **99** (2019) 012515

updated in K. Gaul, R. Berger, *JHEP* **08** (2024) 100

Methods / Packages

P rogram
• for
A tomic
• and
M olecular

D irect
I terative
R elativistic
A ll-electron
C alculations

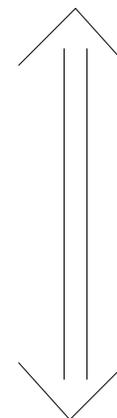


diracprogram.org

KR-CI module

T. F., H.J.Å. Jensen, J. Olsen, L. Visscher, *J Chem Phys* **124** (2006) 104106

S. Knecht, H.J.Å. Jensen, T. F., *J Chem Phys* **132** (2010) 014108



Atomic EDM

in terms of underlying symmetry breaking

Electric dipole moment of an atom:¹⁰

$$d_a := - \lim_{E_{\text{ext}} \rightarrow 0} \left[\frac{\partial(\Delta\varepsilon_{PT})}{\partial E_{\text{ext}}} \right] \quad \Delta\varepsilon_{PT} \text{ is some } P, T\text{-odd energy shift.}$$

Sources are particle EDMs, nuclear MQM, nuclear Schiff moment, \mathcal{T} -odd contribution to weak interaction etc.

For some Hamiltonian $\hat{H}_{PT} = C_{\mathcal{CP}} \hat{O}_{PT}$, we then have

$$d_a = - \lim_{E_{\text{ext}} \rightarrow 0} \frac{\partial}{\partial E_{\text{ext}}} C_{\mathcal{CP}} \langle \hat{O}_{PT} \rangle_{\psi(E_{\text{ext}})}$$

Defining a general interaction constant as $\alpha_{PT} := \frac{d_a}{C_{\mathcal{CP}}}$ the linear-regime atomic interaction constant is then:

$$\alpha_{PT} = - \lim_{E_{\text{ext}} \rightarrow 0} \frac{\langle \hat{O}_{PT} \rangle_{\psi(E_{\text{ext}})}}{E_{\text{ext}}} \approx \alpha_{PT}(\text{lin}) = - \frac{\langle \hat{O}_{PT} \rangle_{\psi(E_{\text{ext}})}}{E_{\text{ext}}}$$

with finite but very small E_{ext} .

¹⁰E.D. Commins, *Adv. Mol. Opt. Phys.* **40** (1999) 1

Atomic and Molecular Correlated Wavefunctions¹¹

Hamiltonians

- Dirac-Coulomb Hamiltonian + external electric field (atoms)

$$\hat{H}^{\text{Dirac-Coulomb}} + \hat{H}^{\text{Int-Dipole}} \\ = \sum_i^n \left[c \boldsymbol{\alpha}_i \cdot \mathbf{p}_i + \beta_i c^2 - \frac{Z}{r_i} \mathbb{1}_4 \right] + \sum_{i,j>j}^n \frac{1}{r_{ij}} \mathbb{1}_4 + \sum_i^n \mathbf{r}_i \cdot \mathbf{E}_{\text{ext}} \mathbb{1}_4$$

- Dirac-Coulomb Hamiltonian operator (molecules)

$$\hat{H}^{DC} = \sum_i^n \left[c \boldsymbol{\alpha}_i \cdot \mathbf{p}_i + \beta_i c^2 - \sum_A^N \frac{Z}{r_{iA}} \mathbb{1}_4 \right] + \sum_{i,j>i}^n \frac{1}{r_{ij}} \mathbb{1}_4 + \sum_{A,B>A}^N V_{AB}$$

- Dirac-Coulomb-Gaunt¹² Hamiltonian operator (molecules)

$$\hat{H}^{DCG} = \sum_i^n \left[c \boldsymbol{\alpha}_i \cdot \mathbf{p}_i + \beta_i c^2 - \sum_A^N \frac{Z}{r_{iA}} \mathbb{1}_4 \right] + \sum_{i,j>i}^n \left(\frac{1}{r_{ij}} \mathbb{1}_4 - \frac{1}{2} \frac{\vec{\alpha}_i \vec{\alpha}_j}{r_{ij}} \right) + \sum_{A,B>A}^N V_{AB}$$

¹¹T. F., H.J.Å. Jensen, J. Olsen, L. Visscher, *J Chem Phys* **124** (2006) 104106

S. Knecht, H.J.Å. Jensen, T. F., *J Chem Phys* **132** (2010) 014108

¹²A. Marc, T.F., in preparation

Calculation of Properties Including \mathcal{P}, \mathcal{T} -Violating Effects¹³

Using String-Based CI Techniques

Solve CI problem $\Rightarrow \psi_k^{(0)}$; expectation value over relativistic Configuration Interaction wavefunction

$$\langle \hat{O} \rangle_{\psi_k^{(0)}} = \sum_{I, J=1}^{\dim \mathcal{F}^t(M, n)} c_{kI}^* c_{kJ} \langle | (\mathcal{S}\bar{\mathcal{T}})_I^\dagger | \hat{O} | (\mathcal{S}\bar{\mathcal{T}})_J | \rangle$$

Property operator \hat{O} in basis of Kramers-paired atomic/molecular spinors

$$\hat{O} = \sum_{i, j=1}^{P_u} o_{ij} a_i^\dagger a_j + \sum_{i=1}^{P_u} \sum_{j=P_u+1}^P o_{i\bar{j}} a_i^\dagger a_{\bar{j}} + \sum_{i=P_u+1}^P \sum_{j=1}^{P_u} o_{\bar{i}j} a_{\bar{i}}^\dagger a_j + \sum_{i, j=P_u+1}^P o_{\bar{i}\bar{j}} a_{\bar{i}}^\dagger a_{\bar{j}}$$

First-term contribution to expectation value

$$O(\Psi_k)_1 = \sum_{I, J=1}^{\dim \mathcal{F}^t(M, n)} c_{kI}^* c_{kJ} \sum_{i, j=1}^{P_u} o_{ij} \langle | \prod_{p=1}^{N_p} \prod_{\bar{p}=N_p+1}^{N_p+N_{\bar{p}}} a_{\bar{p}} a_p a_i^\dagger a_j \prod_{q=1}^{N_p} \prod_{\bar{q}=N_p+1}^{N_p+N_{\bar{p}}} a_q^\dagger a_{\bar{q}}^\dagger | \rangle$$

¹³S. Knecht, Dissertation, HHU Düsseldorf (2009)
T. F., M.K. Nayak, *Phys Rev A* **88** (2013) 032514

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; Dirac-Coulomb Hartree-Fock

Atomic interaction constant¹⁵ as implemented into KRCI/DIRAC¹⁶

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------------------|------------|------------------------|----------|
| QZ/DCHF [17] | -5.980 | 0.0 | 1.0 | 1 |
| Mårtensson-Pendrill [14] (RPA) | -6.0 | 0.0 | | |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0.0 | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

¹⁴A.-M. Mårtensson-Pendrill, *Phys. Rev. Lett.* **54** (1985) 1153

¹⁵E. A. Hinds, C. E. Loving, and P. G. H. Sandars, *J. Phys. B, At. Mol. Phys.* **1** (1968) 499
T.F., *Phys. Rev. A* **99** (2019) 012515

¹⁶S. Knecht and H. J. Aa. Jensen, T.F., *J. Chem. Phys.* **132** (2010) 014108
T. Saue *et al.*, *J. Chem. Phys.* **152** (2020) 204104

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; shell effects

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------------------|-------------|------------------------|--------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD2/8au | -5.271 | 11.9 | 0.981 | 2,474 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

- Partial removal of electron density from most strongly $s - p$ -mixed shell ($6s$)

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; shell effects

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD2/8au | -5.271 | 11.9 | 0.981 | 2,474 |
| QZ/SD12/8au | -5.329 | -1.0 | 0.958 | 131,111 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

- Net removal of electron density from non-contributing shells (d, f, \dots)

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

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Hg atom; shell effects

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD2/8au | -5.271 | 11.9 | 0.981 | 2, 474 |
| QZ/SD12/8au | -5.329 | -1.0 | 0.958 | 131, 111 |
| QZ/SD20/8au | -5.240 | 1.5 | 0.955 | 390,929 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

- Partial removal of electron density from directly contributing shells (5s, 5p)

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; shell effects

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [$10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm}$] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|------------------------------------------------------------------------------|-------------|------------------------|------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD2/8au | -5.271 | 11.9 | 0.981 | 2, 474 |
| QZ/SD12/8au | -5.329 | -1.0 | 0.958 | 131, 111 |
| QZ/SD20/8au | -5.240 | 1.5 | 0.955 | 390, 929 |
| QZ/SD34/8au | -5.307 | -1.1 | 0.955 | 1,046,374 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

- Net removal of electron density from non-contributing shells (d, f, \dots)

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; shell effects

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD2/8au | -5.271 | 11.9 | 0.981 | 2, 474 |
| QZ/SD12/8au | -5.329 | -1.0 | 0.958 | 131, 111 |
| QZ/SD20/8au | -5.240 | 1.5 | 0.955 | 390, 929 |
| QZ/SD34/8au | -5.307 | -1.1 | 0.955 | 1, 046, 374 |
| QZ/SD44/8au | -5.340 | -0.6 | 0.955 | 1,770,973 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

- Net removal of electron density from non-contributing shells (d, f, \dots)

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; higher-rank correlations

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD12/8au | -5.329 | 10.9 | 0.958 | 131,111 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; higher-rank correlations

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD12/8au | -5.329 | 10.9 | 0.958 | 131, 111 |
| QZ/SD10_SDT12/8au | -4.875 | 7.6 | 0.953 | 10,428,991 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; higher-rank correlations

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD12/8au | -5.329 | 10.9 | 0.958 | 131, 111 |
| QZ/SD10_SDT12/8au | -4.875 | 7.6 | 0.953 | 10, 428, 991 |
| QZ/SDT12/8au | -4.884 | -0.2 | 0.951 | 22,344,077 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; higher-rank correlations

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|----------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD12/8au | -5.329 | 10.9 | 0.958 | 131, 111 |
| QZ/SD10_SDT12/8au | -4.875 | 7.6 | 0.953 | 10, 428, 991 |
| QZ/SDT12/8au | -4.884 | -0.2 | 0.951 | 22, 344, 077 |
| QZ/SDT10_SDTQ12/8au | -4.555 | 5.5 | 0.939 | 1,192,109,441 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; higher-rank correlations

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|----------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD12/8au | -5.329 | 10.9 | 0.958 | 131, 111 |
| QZ/SD10_SDT12/8au | -4.875 | 7.6 | 0.953 | 10, 428, 991 |
| QZ/SDT12/8au | -4.884 | -0.2 | 0.951 | 22, 344, 077 |
| QZ/SDT10_SDTQ12/8au | -4.555 | 5.5 | 0.939 | 1, 192, 109, 441 |
| QZ/SDTQ12/8au | -4.611 | -0.9 | | 2,039,321,099 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; cutoff in virtual complement

$$\alpha_{C_T} := \frac{\Delta\varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F\sqrt{2}\langle\Sigma\rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle\Sigma\rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------|------------|------------------------|--------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10, 428, 991 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
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Hg atom; cutoff in virtual complement

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10,428,991 |
| QZ/SD10_SDT12/10au | -4.906 | -0.5 | 0.953 | 20,903,097 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; cutoff in virtual complement

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10,428,991 |
| QZ/SD10_SDT12/10au | -4.906 | -0.5 | 0.953 | 20,903,097 |
| QZ/SD10_SDT12/15au | -4.911 | -0.1 | 0.953 | 23,359,445 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; cutoff in virtual complement

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10,428,991 |
| QZ/SD10_SDT12/10au | -4.906 | -0.5 | 0.953 | 20,903,097 |
| QZ/SD10_SDT12/15au | -4.911 | -0.1 | 0.953 | 23,359,445 |
| QZ/SD10_SDT12/20au | -4.915 | -0.1 | 0.953 | 32,027,149 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; cutoff in virtual complement

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|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10,428,991 |
| QZ/SD10_SDT12/10au | -4.906 | -0.5 | 0.953 | 20,903,097 |
| QZ/SD10_SDT12/15au | -4.911 | -0.1 | 0.953 | 23,359,445 |
| QZ/SD10_SDT12/20au | -4.915 | -0.1 | 0.953 | 32,027,149 |
| QZ/SD10_SDT12/40au | -4.916 | -0.0 | 0.953 | 40,795,699 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; cutoff in virtual complement

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|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|-------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDT12/8au | -4.875 | 18.5 | 0.953 | 10,428,991 |
| QZ/SD10_SDT12/10au | -4.906 | -0.5 | 0.953 | 20,903,097 |
| QZ/SD10_SDT12/15au | -4.911 | -0.1 | 0.953 | 23,359,445 |
| QZ/SD10_SDT12/20au | -4.915 | -0.1 | 0.953 | 32,027,149 |
| QZ/SD10_SDT12/40au | -4.916 | -0.0 | 0.953 | 40,795,699 |
| QZ/SD10_SDT12/100au | -4.916 | -0.0 | 0.953 | 61,989,103 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; inner shells and higher ranks

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|------------------------------------|---------------------------------------------------------------------------|------------|------------------------|---------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDTQ12/8au | -4.715 | 21.2 | 0.945 | 200, 724, 571 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|--------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDTQ12/8au | -4.715 | 21.2 | 0.945 | 200, 724, 571 |
| QZ/S8_SD10_SDTQ20/8au | -4.398 | 5.3 | | 565,912,481 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; inner shells and higher ranks

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|--------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDTQ12/8au | -4.715 | 21.2 | 0.945 | 200, 724, 571 |
| QZ/S8_SD10_SDTQ20/8au | -4.398 | 5.3 | | 565, 912, 481 |
| QZ/SD8_SD10_SDTQ20/8au | -4.408 | -0.2 | | 699,625,055 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; inner shells and higher ranks

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|----------------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD10_SDTQ12/8au | -4.715 | 21.2 | 0.945 | 200, 724, 571 |
| QZ/S8_SD10_SDTQ20/8au | -4.398 | 5.3 | | 565, 912, 481 |
| QZ/S8_SDT10_SDTQ20/8au | -4.13 | 4.5 | | 4,567,808,033 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; inner shells and cutoff

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| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|------------|------------------------|----------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD20/8au | -5.240 | 12.4 | 0.955 | 390, 929 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; inner shells and cutoff

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| Model [17] | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------------------|-------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD20/8au | -5.240 | 12.4 | 0.955 | 390,929 |
| QZ/SD20/10au | -5.342 | -1.7 | | 604,983 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

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Hg atom; inner shells and cutoff

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------------------|------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD20/8au | -5.240 | 12.4 | 0.955 | 390, 929 |
| QZ/SD20/10au | -5.342 | -1.7 | | 604, 983 |
| QZ/SD20/15au | -5.337 | 0.1 | | 655,433 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; inner shells and cutoff

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | α_{C_T} [10 ⁻²⁰ $\langle \Sigma \rangle_{\text{Hg}}$ ecm] | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|-----------------------------------------------------------------------------|-------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD20/8au | -5.240 | 12.4 | 0.955 | 390, 929 |
| QZ/SD20/10au | -5.342 | -1.7 | | 604, 983 |
| QZ/SD20/15au | -5.337 | 0.1 | | 655, 433 |
| QZ/SD20/20au | -5.348 | -0.2 | | 806,331 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

Hg atom; inner shells and cutoff

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \imath \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [17] | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ | $C_{\text{Hg}_{6s^2}}$ | dim. |
|------------------------------------|---------------------------------------------------------------------------------------|-------------|------------------------|----------------|
| QZ/DCHF | -5.980 | 0. | 1.0 | 1 |
| QZ/SD20/8au | -5.240 | 12.4 | 0.955 | 390, 929 |
| QZ/SD20/10au | -5.342 | -1.7 | | 604, 983 |
| QZ/SD20/15au | -5.337 | 0.1 | | 655, 433 |
| QZ/SD20/20au | -5.348 | -0.2 | | 806, 331 |
| QZ/SD20/40au | -5.352 | -0.1 | | 951,795 |
| Dzuba <i>et al.</i> [18] (RPA) | -5.9 | 0. | | |
| Dzuba <i>et al.</i> [18] (CI+MBPT) | -5.1 | 13.6 | | |

¹⁷L. V. Skripnikov, T. F., (2026) *unpublished*

¹⁸V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

Search for Semi-Hadronic-Source EDM: TPT-Ne Interaction

¹⁹⁹Hg

$$\alpha_{C_T} := \frac{\Delta \varepsilon_{C_T}}{C_T E_{\text{ext}}} = \frac{G_F \sqrt{2} \langle \Sigma \rangle_A}{E_{\text{ext}}} \left\langle \nu \sum_{j=1}^n (\gamma_3)_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}$$

| Model [19] | $\alpha_{C_T} \left[10^{-20} \langle \Sigma \rangle_{\text{Hg}} \text{ ecm} \right]$ | $\Delta\%$ corr. |
|----------------------------------------------|---------------------------------------------------------------------------------------|------------------|
| T. F. DCHF | -5.98 | |
| Skripnikov DCHF | -5.98 | |
| T. F. CI current best | -4.13 | 31 |
| Skripnikov CC current best | -3.83 | 36 |
| Dzuba <i>et al.</i> [20] (RPA) | -5.9 | |
| Dzuba <i>et al.</i> [20] (CI+MBPT) | -5.1 | 13.6 |
| Singh <i>et al.</i> [21] CCSD _p T | -4.3 | |
| Sahoo <i>et al.</i> [22] RNCCSD | -3.3 | |

¹⁹L. V. Skripnikov, T. F. (2026) *unpublished*

²⁰V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

²¹Y. Singh and B. K. Sahoo, *Phys. Rev. A* **91** (2015) 030501(R)

²²B. K. Sahoo, B. P. Das, *Phys. Rev. Lett.* **120** (2018) 203001

Search for Hadron-Source EDM: Schiff-Moment Interaction

¹⁹⁹Hg atom

Atomic interaction constant²³ as implemented into KRCI/DIRAC²⁴

$$\alpha_{\text{SM}} := \frac{\Delta \varepsilon_{\text{SM}}}{S_z E_{\text{ext}}} = \frac{-\frac{3}{B} \left\langle \sum_{j=1}^n \hat{z}_j \rho(\mathbf{r}_j) \right\rangle_{\psi(E_{\text{ext}})}}{E_{\text{ext}}}$$

| Model | $\alpha_{\text{SM}} \left[10^{-17} \frac{\text{ecm}}{\text{efm}^3} \right]$ | $ \Delta\% $ corr. |
|------------------------------------------|------------------------------------------------------------------------------|--------------------|
| Fleig DCHF | -2.89 | |
| Skripnikov DCHF | -2.90 | |
| Fleig CI current best | -2.26 | 21.8% |
| Skripnikov CC current best | -1.88 | 35.2% |
| Dzuba <i>et al.</i> [25] (RPA, 2009) | -3.0 | |
| Dzuba <i>et al.</i> [25] (CI+MBPT, 2009) | -2.6 | 13.3% |

²³V. A. Dzuba, V. V. Flambaum, J. S. M. Ginges, and M. G. Kozlov, *Phys. Rev. A* **66** (2002) 021111

M. Hubert, T.F., *Phys. Rev. A* **106** (2022) 022817

²⁴S. Knecht and H. J. Aa. Jensen, T.F., *J. Chem. Phys.* **132** (2010) 014108

T. Saue *et al.*, *J. Chem. Phys.* **152** (2020) 204104

²⁵V. A. Dzuba, V. V. Flambaum, S. G. Porsev, *Phys. Rev. A* **80** (2009) 032120

EDM Science

- Electron EDM interactions (HfF^+ , ThO , Hg , Tl , TaO^+ , RaAg et al.)

T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

T. F., L. V. Skripnikov, *Symmetry* **12** (2020) 498

T. F., M. Jung, *J High Energy Phys. (JHEP)* **07** (2018) 012

T. F., *Phys. Rev. A* **96** (2017) 040502(R)

T. F., *Phys. Rev. A* **95** (2017) 022504

M. Denis, T. F., *J. Chem. Phys.* **145** (2016) 214307

- Nuclear Schiff-moment interactions (Xe , Hg , TlF , FrAg et al.)

A. Marc, M. Hubert, T. F., *Phys. Rev. A* **108** (2023) 062815

M. Hubert, T. F., *Phys. Rev. A* **106** (2022) 022817

- Weak neutral current interactions (Xe , Hg , Ra , TlF , FrAg , CsAg)

L. V. Skripnikov, T. F. (2026) *in preparation*

A. Marc, T. F., *Eur. Phys. J. D* **79** (2025) 19

T. F., *Phys. Rev. A* **109** (2024) 022807

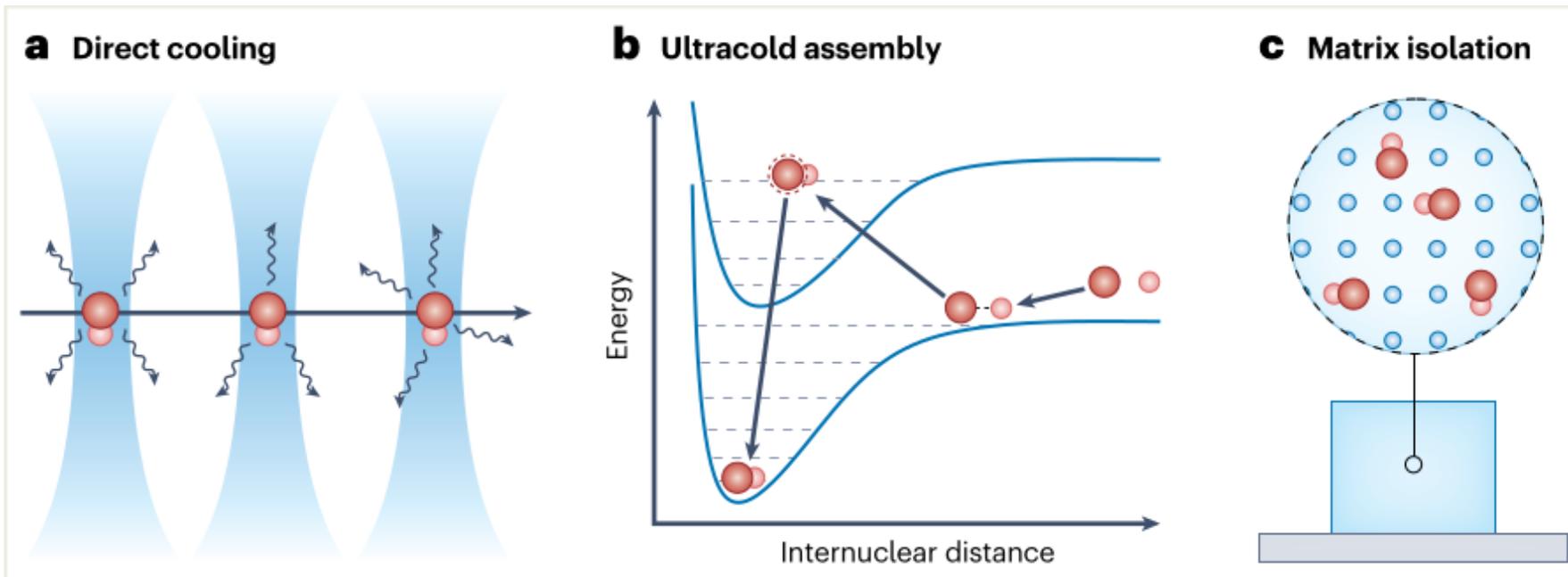
T. F., *Phys. Rev. A* **99** (2019) 012515

- Nuclear MQM interactions (TaN , TaO^+ , HfF^+ , RaAg)

T. F., M. K. Nayak, M. G. Kozlov, *Phys. Rev. A* **93** (2016) 012505

EDM Search with Assembled Ultracold Molecules

D. DeMille, N. R. Hutzler, A. M. Rey, T. Zelevinsky, *Nat. Phys.* **20** (2024) 741



FrAg J. Kłos, H. Li, E. Tiesinga, S. Kotochigova, *New J. Phys.* **24** (2022) 025005

RaAg T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Schiff moment in terms of QCD $\bar{\theta}$ and π -meson–nucleon CP-violating interaction constants²⁶

$$\begin{aligned} S(^{223}\text{Fr}) &\approx (-4.16 g\bar{g}_0 + 20.64 g\bar{g}_1 - 11.04 g\bar{g}_2) \text{ efm}^3 \\ S(^{205}\text{Tl}) &\approx (0.13 g\bar{g}_0 - 0.004 g\bar{g}_1 - 0.27 g\bar{g}_2) \text{ efm}^3 \\ S(^{225}\text{Ra}) &\approx (-2.6 g\bar{g}_0 + 12.9 g\bar{g}_1 - 6.9 g\bar{g}_2) \text{ efm}^3 \end{aligned}$$

$$\begin{aligned} S(^{223}\text{Fr}) &\approx -1.6 \bar{\theta} e \text{ fm}^3 \\ S(^{205}\text{Tl}) &\approx 0.02 \bar{\theta} e \text{ fm}^3 \\ S(^{225}\text{Ra}) &\approx -\bar{\theta} e \text{ fm}^3 \end{aligned}$$

^{223}Fr orders of magnitude more sensitive than ^{205}Tl

²⁶V. V. Flambaum, V. A. Dzuba, and H. B. Tran Tan, *Phys. Rev. A* **101** (2020) 042501
V. A. Dzuba, V. V. Flambaum, *Phys. Rev. A* **101** (2020) 042504

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Atomic Basis Sets / Hartree-Fock Theory

Molecular Schiff-moment interaction Hamiltonian²⁷

$$W_{SM}(A) := \frac{\Delta\varepsilon_{SM}(A)}{S_z(A)} = -\frac{3}{B} \left\langle \sum_{j=1}^n \hat{z}_j \rho_A(\mathbf{r}_j) \right\rangle_{\psi}$$

as implemented into KRCI/DIRAC²⁸

| Basis | CsLi ($R_e = 6.927$ a.u.) | | FrAg ($R_e = 6.190$ a.u.) | |
|-------|-----------------------------|-----------------|-----------------------------|-----------------|
| | ε_{DCHF} [a.u.] | W_{SM} [a.u.] | ε_{DCHF} [a.u.] | W_{SM} [a.u.] |
| cvDZ | -7794.1925854 | -10110 | -29622.7980959 | 5946 |
| cvTZ | -7794.2033064 | -2849 | -29622.8345496 | 28173 |
| cvQZ | -7794.2038442 | 2098 | -29622.8362766 | 29451 |
| cvQZ+ | -7794.2038394 | 2887 | -29622.8354238 | 31350 |

²⁷V. A. Dzuba, V. V. Flambaum, J. S. M. Ginges, and M. G. Kozlov, *Phys. Rev. A* **66** (2002) 021111

²⁸M. Hubert, T.F., *Phys. Rev. A* **106** (2022) 022817

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Electron Correlation Effects

| Basis/cutoff | ε_{CI} [a.u.] | W_{SM} [a.u.] |
|-----------------|----------------------------------|------------------------|
| cvQZ+/DCHF | -29622.8354238 | 31350 |
| cvQZ+/SD2_2au | -29622.8604657 | 30359 |
| cvQZ+/SD2_5au | -29622.8605445 | 30355 |
| cvQZ+/SD2_8au | -29622.8605500 | 30360 |
| cvQZ+/SD10_8au | -29623.0196812 | 29980 |
| cvQZ+/SDT10_8au | -29623.0260848 | 29909 |
| cvQZ+/SD12_8au | -29623.1920759 | 30711 |
| cvQZ+/SD20_8au | -29623.3371101 | 30127 |
| cvQZ+/SD36_5au | -29623.7102434 | 30333 |
| cvQZ+/SD36_8au | -29623.8379481 | 30239 |

- SD36 model includes Fr($7s, 6p, 6s, 5d$) and Ag($5s, 4d, 4p$) shells
- Excitations out of Fr(s, p) shells diminish W_{SM} .
- Excitations out of other shells increase W_{SM} .

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Comparison with other $^1\Sigma_0$ molecules

| | Z (heavy) | EA (light) [eV] | W_{SM} [a.u.] (at respective R_e) |
|------|-------------|-----------------|--------------------------------------------------------------------------|
| CsAg | 55 | 1.304 | 3530 ²⁹ |
| FrLi | 87 | 0.618 | 24414 ²⁹ |
| FrAg | 87 | 1.304 | 30168 ± 2504 ²⁹ |
| TIF | 81 | 3.401 | 39967 ± 3600 ³⁰ 37192 ³¹ 40539 ³² |

- Cs → Fr order of magnitude gain
- Li → Ag substantial gain
- TIF benefits from huge EA(F)

²⁹A. Marc, M. Hubert, T. F., *Phys. Rev. A* **108** (2023) 062815

³⁰M. Hubert, T.F., *Phys. Rev. A* **106** (2022) 022817

³¹L. V. Skripnikov, N. S. Mosyagin, A. V. Titov, and V. V. Flambaum, *Phys. Chem. Chem. Phys.* **22** (2020) 18374

³²V. V. Flambaum, V. A. Dzuba, and H. B. Tran Tan, *Phys. Rev. A* **101** (2020) 042501

A. N. Petrov, N. S. Mosyagin, T. A. Isaev, A. V. Titov, V. F. Ezhov, E. Eliav, and U. Kaldor, *Phys. Rev. Lett.* **88** (2002) 073001

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Atomic Basis Sets / Hartree-Fock Theory

Molecular TPT-Ne interaction Hamiltonian³³

$$W_T(A) = \sqrt{2}G_F \langle \Sigma \rangle_A \left\langle \psi^{(0)} \left| i \sum_{j=1}^n (\gamma_3)_j \rho_A(\mathbf{r}_j) \right| \psi^{(0)} \right\rangle$$

as implemented into KRCI/DIRAC³⁴

| Basis/model | ε_{CI} [a.u.] | $W_T(\text{Fr})$ [$10^{-13} \langle \Sigma \rangle_A$ a.u.] |
|-------------|----------------------------------|--------------------------------------------------------------|
| cvDZ/DCHF | -29622.8235344 | 4.109 |
| cvTZ/DCHF | -29622.8356809 | 4.148 |
| cvQZ/DCHF | -29622.8363746 | 4.150 |
| cvQZ+/DCHF | -29622.8354238 | 4.151 |

³³E. A. Hinds, C. E. Loving, and P. G. H. Sandars, *J. Phys. B, At. Mol. Phys.* **1** (1968) 499

³⁴T.F., *Phys. Rev. A* **109** (2024) 022807

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Correlation Effects

$$W_T(A) = \sqrt{2}G_F \langle \Sigma \rangle_A \left\langle \psi^{(0)} \left| i \sum_{j=1}^n (\gamma_3)_j \rho_A(\mathbf{r}_j) \right| \psi^{(0)} \right\rangle$$

| Basis/model | ϵ_{CI} [a.u.] | $W_T(\text{Fr})$ [$10^{-13} \langle \Sigma \rangle_A$ a.u.] |
|------------------------------|-------------------------------|--------------------------------------------------------------|
| cvQZ/DCHF | -29622.8363746 | 4.150 |
| cvQZ/SD2_8a.u. | -29622.8615002 | 4.013 |
| cvQZ/SD10_3a.u. | -29623.0079474 | 4.041 |
| cvQZ/SD10_cc | -29623.0157765 | 4.013 |
| cvQZ/SD10_8a.u. | -29623.0206732 | 4.015 |
| cvQZ/SD10_11.5a.u. | -29623.0210675 | 4.013 |
| cvQZ/SD8_SDT10_3a.u. | -29623.0100912 | 4.045 |
| cvQZ/SD8_SDTQ10_3a.u. | -29623.0171368 | 3.941 |
| cvQZ/SD8_SDT10_cc | -29623.0179520 | 4.021 |
| cvQZ/SD12_8a.u. | -29623.1930035 | 4.050 |
| cvQZ/SD20_8a.u. | -29623.3380747 | 4.007 |
| cvQZ/SD36_8a.u. | -29623.8389564 | 4.018 |

Search for Hadron-Source EDM: Francium-Silver (FrAg)

Sensitivity Ratios [35]

$$\tilde{M} := \frac{W_{SM}(A)}{W_T(A)} = \frac{-\frac{3}{B} \left\langle \sum_{j=1}^n \hat{z}_j \rho_A(\mathbf{r}_j) \right\rangle_{\psi}}{\sqrt{2} G_F \langle \Sigma \rangle_A \left\langle \psi^{(0)} \left| i \sum_{j=1}^n (\gamma_3)_j \rho_A(\mathbf{r}_j) \right| \psi^{(0)} \right\rangle}$$

| System | W_{SM} [a.u.] | W_T [$10^{-13} \langle \Sigma \rangle_A$ a.u.] | \tilde{M} [$10^{13} \langle \Sigma \rangle_A^{-1}$ a.u.] | I_A | M [10^{13} a.u.] |
|---------------------|-----------------|---------------------------------------------------|-------------------------------------------------------------|-------|-----------------------|
| $^{223}\text{FrAg}$ | 30168 | 3.93 | 7676 | 3/2 | 5117 |
| $^{133}\text{CsAg}$ | 3529.6 | 0.374 | 9437 | 7/2 | 2697 |
| ^{205}TlF | 40539 [36] | 6.25 [37] | 6486 | 1/2 | 12972 |

³⁵A. Marc, T. F., *Eur. J. Phys. D* **79** (2025) 19

³⁶O. Grasdijk et al., *Quantum Sci. Technol.* **6** (2021) 044007

³⁷T. F., *Phys. Rev. A* **109** (2024) 022807

Schiff-Moment, TPT-Ne Interactions and Method Development



Mickaël Hubert, Lecturer

Schiff-moment interaction implementation

Basis sets



Aurélien Marc

Schiff-moment interaction calculations in molecules

TPT-Ne interaction calculations in molecules

DCG-GASCI

Thanks for your attention !

EDM Science

- Electron EDM interactions (HfF⁺, ThO, Hg, Tl, TaO⁺, RaAg et al.)

T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

T. F., L. V. Skripnikov, *Symmetry* **12** (2020) 498

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T. F., *Phys. Rev. A* **96** (2017) 040502(R)

T. F., *Phys. Rev. A* **95** (2017) 022504

M. Denis, T. F., *J. Chem. Phys.* **145** (2016) 214307

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A. Marc, M. Hubert, T. F., *Phys. Rev. A* **108** (2023) 062815

M. Hubert, T. F., *Phys. Rev. A* **106** (2022) 022817

- Weak neutral current interactions (Xe, Hg, Ra, TlF, FrAg, CsAg)

L. V. Skripnikov, T. F. (2026) *in preparation*

A. Marc, T. F., *Eur. Phys. J. D* **79** (2025) 19

T. F., *Phys. Rev. A* **109** (2024) 022807

T. F., *Phys. Rev. A* **99** (2019) 012515

- Nuclear MQM interactions (TaN, TaO⁺, HfF⁺, RaAg)

T. F., M. K. Nayak, M. G. Kozlov, *Phys. Rev. A* **93** (2016) 012505

Towards Ultracold DLT EDM Measurement³⁵

Picking the cherry

Target atom:

$$Z(\text{Ra}) = 88 \quad \alpha_D(\text{Ra}) = 246 \pm 4 \text{ a.u.}^{36}$$

Polarizing partner:

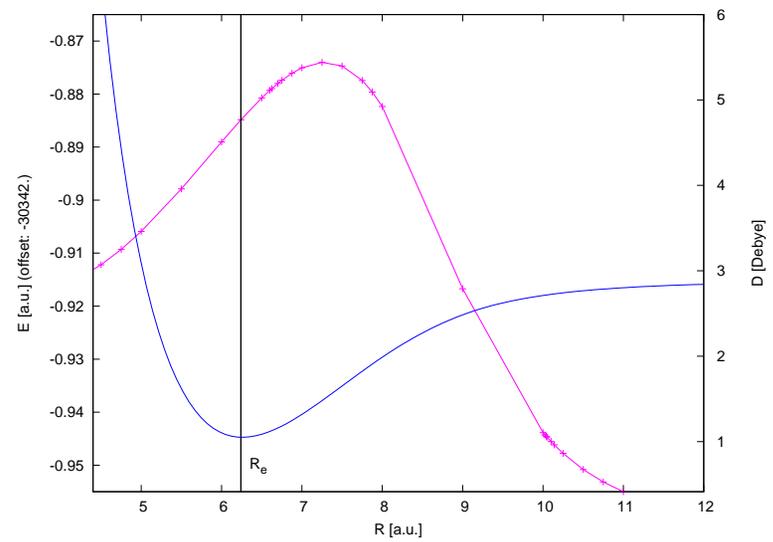
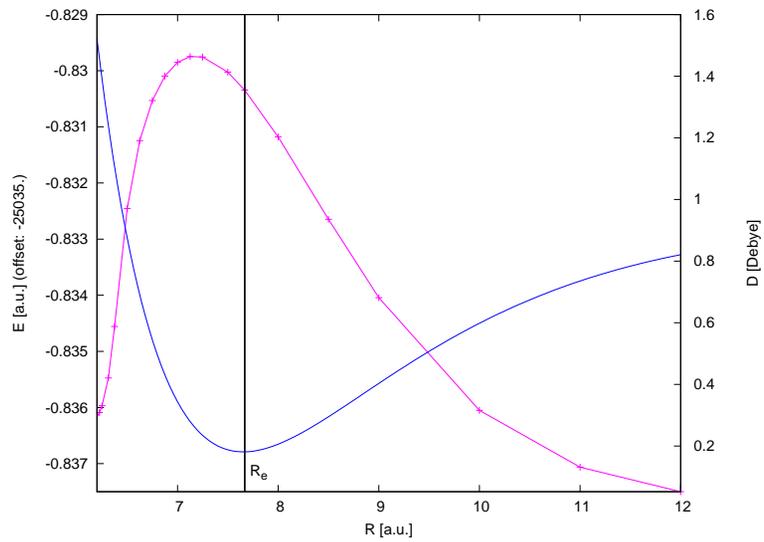
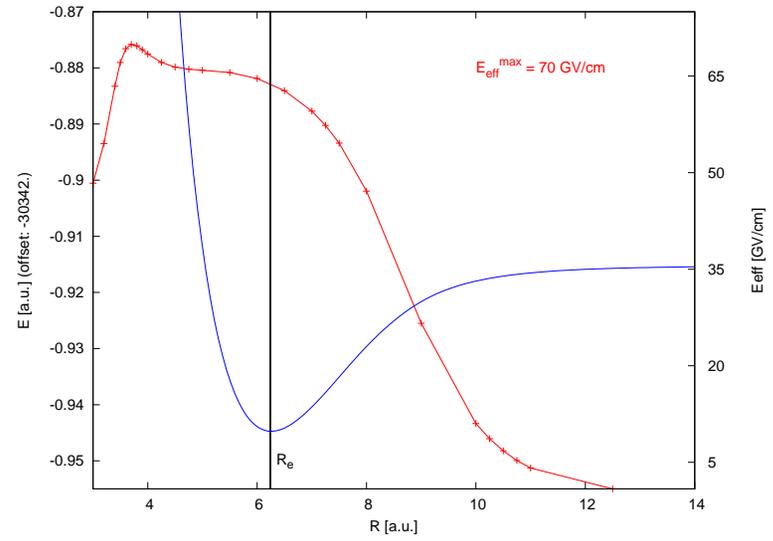
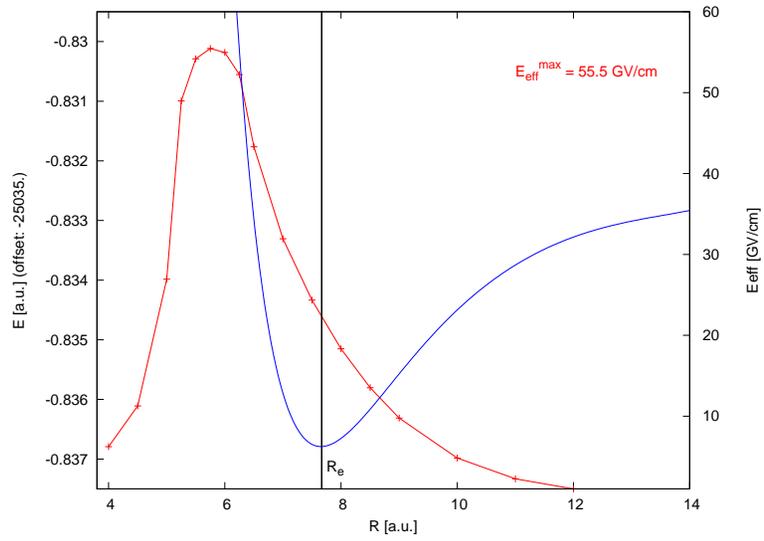
Alkali(-like) atoms: Li, Na, K, Rb, Cs, Fr; Cu, Ag, Au

| | R_e [a.u.] | B_e [cm^{-1}] | D [Debye] | EA [eV] | E_{eff} [$\frac{\text{GV}}{\text{cm}}$] | W_S [kHz] | E_{pol} [$\frac{\text{kV}}{\text{cm}}$] |
|------|--------------|----------------------------|-------------|--------------|----------------------------------------------------|---------------|----------------------------------------------------|
| RaLi | 7.668 | 0.151 | 1.36 | 0.618 | 22.2 | -59.5 | 13.3 |
| RaNa | 8.703 | 0.038 | 0.51 | 0.548 | 12.0 | -32.2 | 8.90 |
| RaK | 10.37 | 0.017 | 0.39 | 0.501 | 5.44 | -14.6 | 5.18 |
| RaRb | 10.75 | 0.008 | 0.36 | 0.486 | 5.01 | -13.6 | 2.75 |
| RaCs | 11.25 | 0.006 | 0.46 | 0.472 | 4.52 | -12.6 | 1.48 |
| RaFr | 11.26 | 0.004 | 0.24 | 0.486 | 3.44 | -12.4 | 2.06 |
| RaCu | 6.050 | 0.033 | 4.30 | 1.236 | 67.0 | -180.6 | 0.92 |
| RaAg | 6.241 | 0.021 | 4.76 | 1.304 | 63.9 | -175.1 | 0.53 |
| RaAu | 5.836 | 0.017 | 5.71 | 2.309 | 50.4 | -166.4 | 0.36 |

³⁵T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

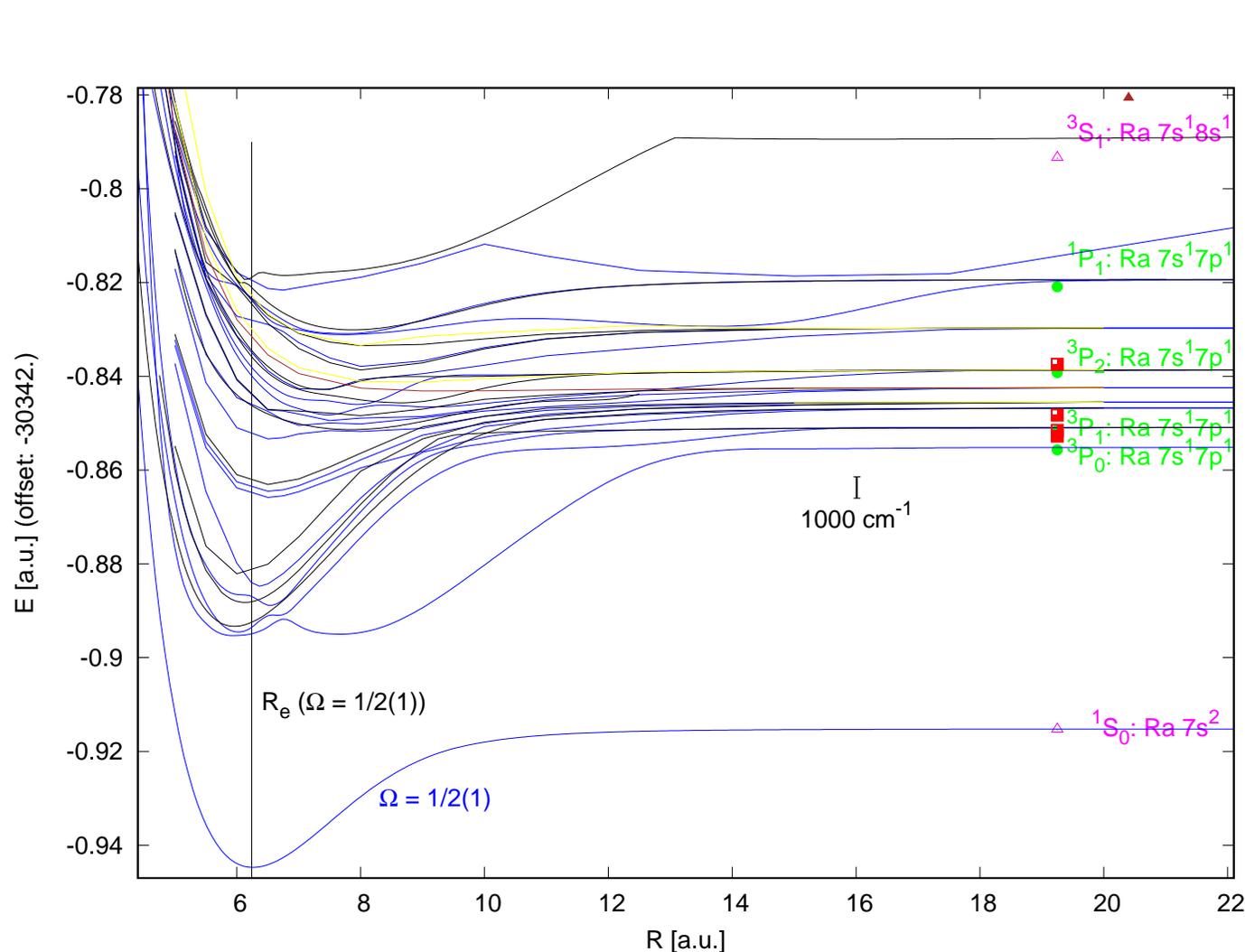
³⁶P. Schwerdtfeger, J. K. Nagle, *Mol. Phys.* **117** (2019) 1200

RaLi vs. RaAg³⁷



³⁷T. F., D. DeMille, *New J. Phys.* **23** (2021) 113039

1) RaAg: Complete Spectrum up to $T \approx 5$ eV (TZ basis)



| | accumulated # of electrons | |
|------------------------------------------------------|-------------------------------|------|
| | min. | max. |
| Virtuals < 4 a.u. (71) | 135 | 135 |
| Valence Ra: 7s,7p,8s,6d,8p Ag: 5s,5p,6s | 133 | 135 |
| Sub-valence Ra: 6s,6p Ag: 4d | 131 | 132 |
| Frozen core | 114 | 114 |

$$D_e(1/2(1)) \approx 0.83 \text{ eV}$$

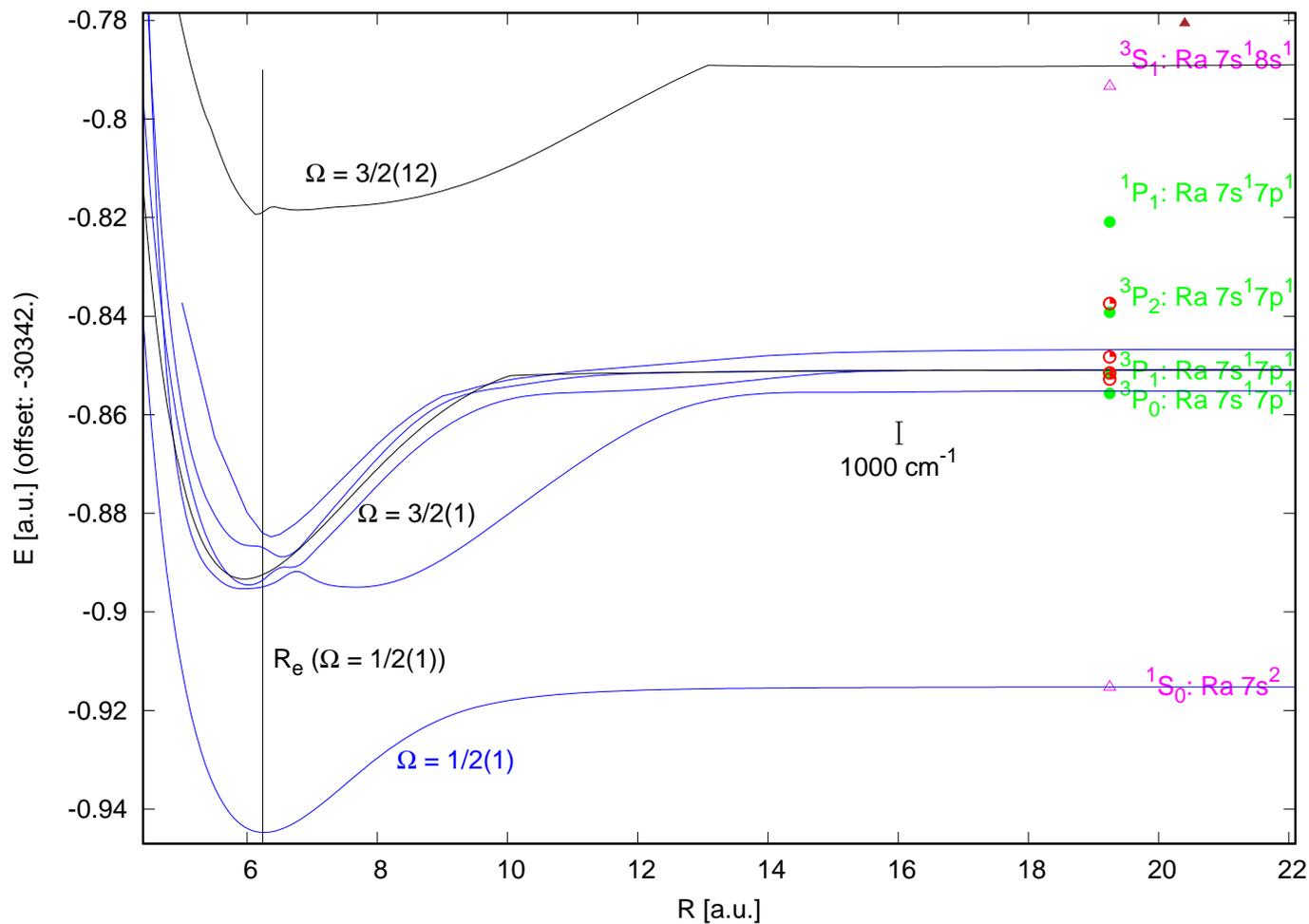
$$D_e(\text{KRb}) \approx 0.52 \text{ eV}^{26}$$

$$D_e(\text{YbRb}) \approx 0.11 \text{ eV}^{27}$$

²⁶S. Kasahara, C. Fujiwara, N. Okada, H. Katô, M. Baba, *J. Chem. Phys.* **111** (1999) 8857

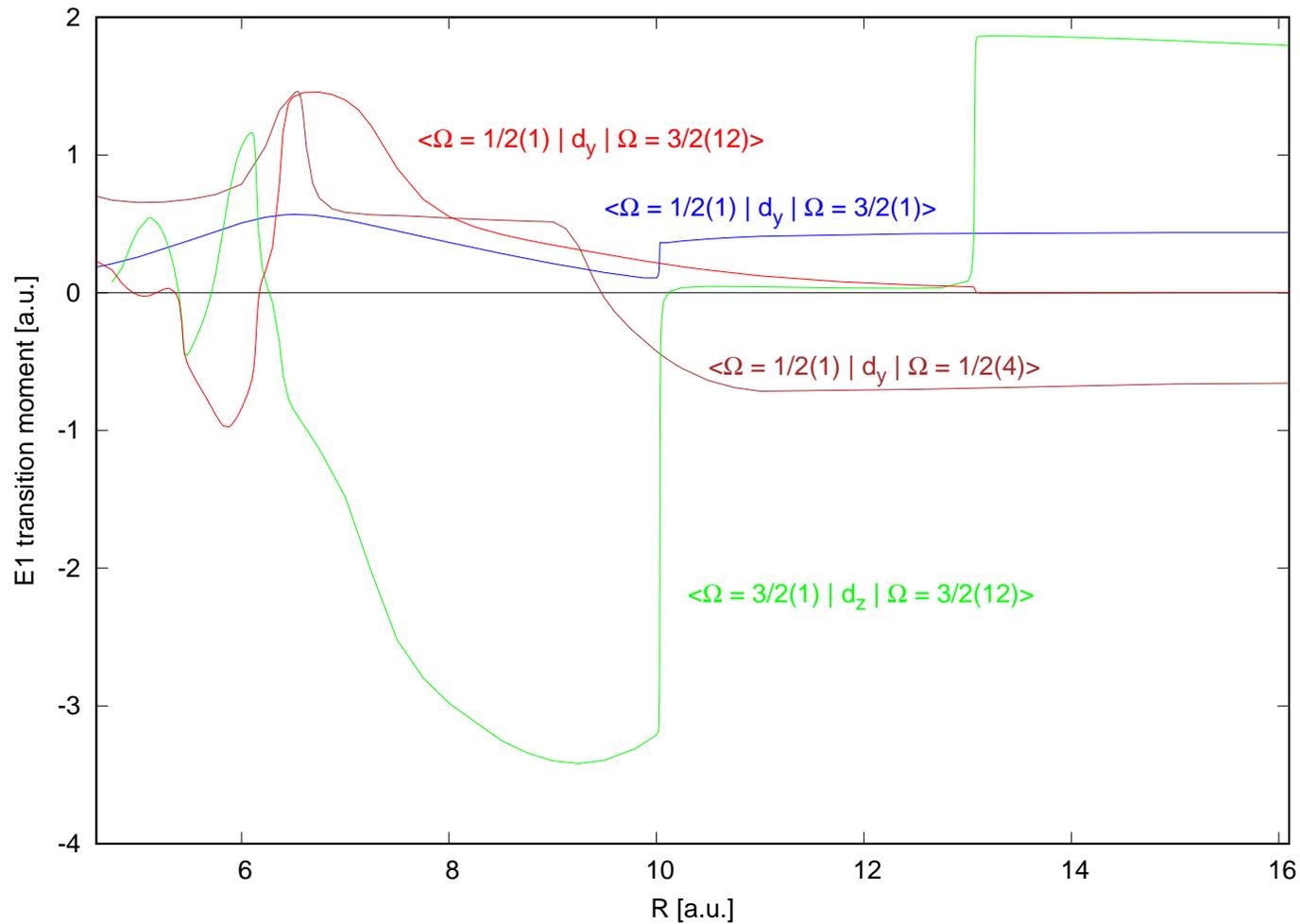
²⁷L. K. Sørensen, S. Knecht, T. F., C. M. Marian, *J. Phys. Chem A* **113** (2009) 12607

1) RaAg: Relevant States $T \approx 5$ eV (TZ basis)



| | accumulated # of electrons | |
|------------------------------------------------------|-------------------------------|------|
| | min. | max. |
| Virtuals < 4 a.u. (71) | 135 | 135 |
| Valence Ra: 7s,7p,8s,6d,8p Ag: 5s,5p,6s | 133 | 135 |
| Sub-valence Ra: 6s,6p Ag: 4d | 131 | 132 |
| Frozen core | 114 | 114 |

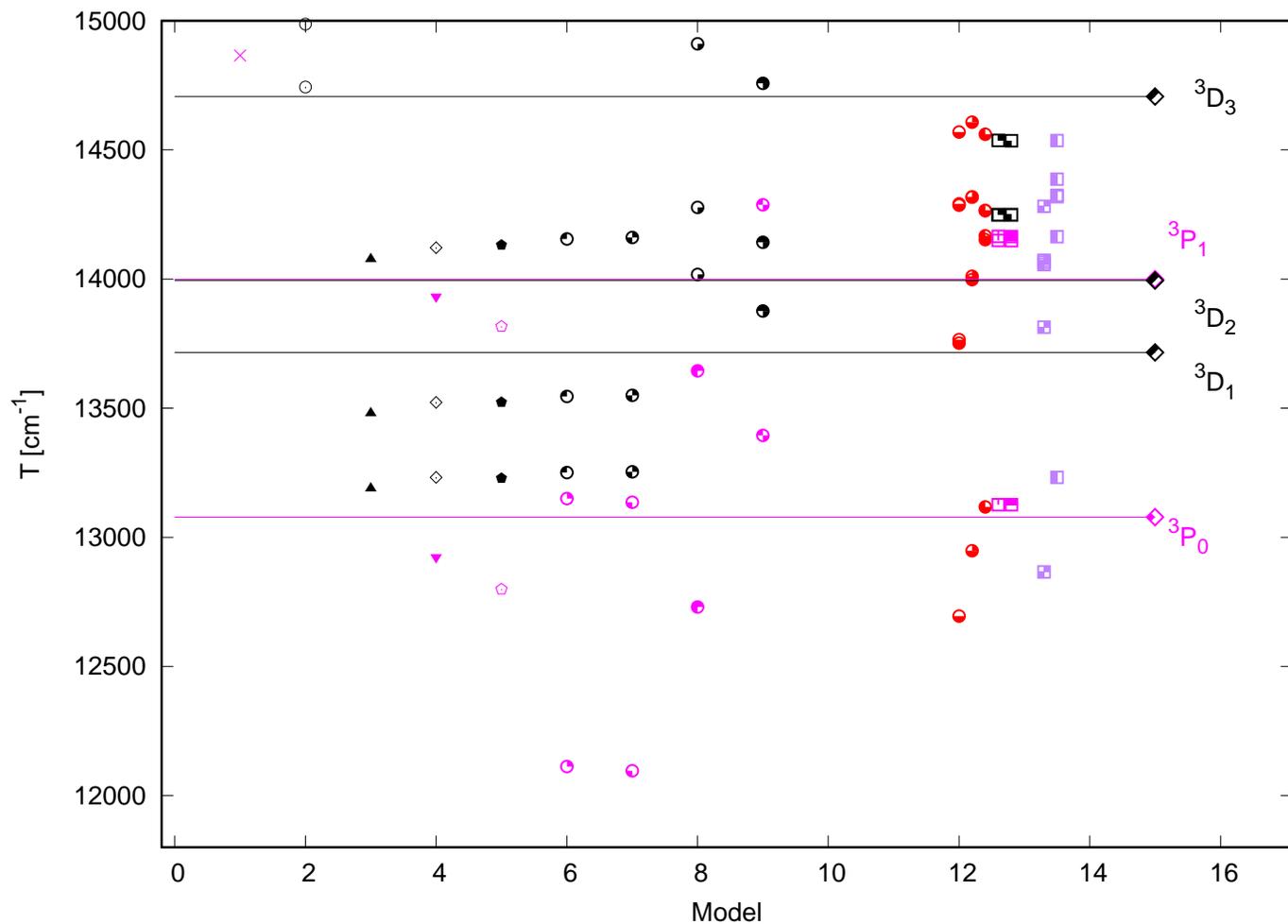
1) RaAg^{40} : E1 TDM $d_{XY}(R) = \left\langle \Psi_X \left| \sum_j q_j \hat{\mathbf{r}}_j \right| \Psi_Y \right\rangle (R)$



Then: $d_{v,v'} = \int_R \psi_{vX}(R) d_{XY}(R) \psi_{v'Y}(R) dR$

⁴⁰T. Fleig, O. Grasdijk, D. DeMille (2024)

2) RaAg: Limited Spectrum up to $T \approx 3$ eV (QZ basis)



| | accumulated # of electrons | |
|-----------------------------------------|-------------------------------|------|
| | min. | max. |
| <i>Virtuals < 4 a.u. (141)</i> | 135 | 135 |
| <i>Ra: 7p,8s,6d,8p,9s Ag: 5p,6s</i> | 133 | 135 |
| <i>Ra: 7s Ag: 5s</i> | 132 | 135 |
| <i>Ra: 6s,6p</i> | 130 | 132 |
| <i>Ag: 4d</i> | 123 | 124 |
| <i>Frozen core</i> | 114 | 114 |

4: SD8_8s6d9s7d7p8pSDT_SD10

12: RaAg (SDT)

9: SD8_8s6d9s7d7p8pSDTQ_SD10

13: RaAg (SDTQ)